

Theoretical study of ArH^+ dissociative recombination and electron-impact vibrational excitation

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ABSTRACT

Cross-sections are presented for dissociative recombination and electron-impact vibrational excitation of the ArH^+ molecular ion at electron energies appropriate for the interstellar environment. The R-matrix method is employed to determine the molecular structure data, i.e. the position and width of the resonance states. The cross-sections and the corresponding Maxwellian rate coefficients are computed using a method based on the Multichannel Quantum Defect Theory. The main result of the paper is the very low dissociative recombination rate found at temperatures below 1000K. This is in agreement with the previous upper limit measurement in merged beams and offers a realistic explanation for the presence of ArH^+ in exotic interstellar conditions.

Key words: interstellar medium – molecular processes.

1 INTRODUCTION

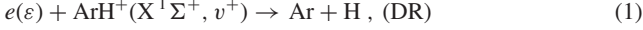
The presence of the ArH^+ molecular cation, argonium, in interstellar medium (ISM) was reported for the first time by Barlow et al. (2013), who detected $^{36}\text{ArH}^+$ 617.525 GHz ($J = 1 - 0$) and 1234.603 GHz ($J = 2 - 1$) emission lines in spectra from the Crab Nebula using the data from Herschel mission. That supernova remnant is known to contain both molecular hydrogen and regions of enhanced ionized argon emission. After this first noble gas molecular ion detection, Schilke et al. (2014) realized that the still unidentified absorption transition at 617.5 GHz observed in diffuse gas towards several sources such as Sg B2, and various PRISMA sources (W31C, W49N, W51e, ...), was, in fact, due to argonium with ^{36}Ar . Moreover, features of $^{38}\text{ArH}^+$ were subsequently found in Sg B2(M) as well and, consequently, Schilke et al. suggested that argonium is ubiquitous in the ISM. More recently, Müller et al. (2015) made extragalactic detections of the ^{36}Ar and ^{38}Ar isotopologues of argonium through absorption studies of a foreground galaxy at $z = 0.89$ along two different lines of sight toward PKS 1830-211 within the band 7 of the ALMA interferometer, including the corresponding redshifted transitions.

The possible formation/destruction processes linked to ArH^+ are discussed by Neufeld & Wolfire (2016) who emphasized that ArH^+ is a good tracer of the almost purely atomic diffuse ISM in the Milky Way. However, an important missing piece of information remains the unknown value of the dissociative recombination rate coefficient of that molecular ion. An upper limit of $10^{-9} \text{ cm}^3 \text{ s}^{-1}$ for electron collision energies below about 2 eV was reported by Mitchell et al. (2005) who performed a storage ring measurement. Mitchell et al. also gave the corresponding theoretical potential curves. That upper limit value is adopted in the presently available astrochemical models for galactic diffuse clouds (Neufeld & Wolfire 2016) whereas Priestley, Barlow & Viti (2017) introduce a lower value ($10^{-11} \text{ cm}^3 \text{ s}^{-1}$) to interpret the Crab nebula observations. Photodissociation of ArH^+ , another potential destruction mechanism, was studied theoretically by Alekseyev, Liebermann & Buenker (2007) and the corresponding photodissociation rate was shown to be moderate, i.e. $9.9 \times 10^{-12} \text{ s}^{-1}$ in the unshielded mean ultraviolet interstellar radiation field (Roueff, Alekseyev & Bourlot 2014; Schilke et al. 2014). In addition to these, the rotational excitation due to electron impact has been studied by Hamilton, Faure & Tennyson (2016).

In this paper, we investigate theoretically the dissociative recombination (DR) process of ArH^+ through *ab initio* methods, including the dependence on the vibrational excitation of the target molecular ion and, in the same energy range, the competitive process of

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vibrational excitation (VE) by electron impact, i.e.:



where ϵ is the incident electron energy, v^+ and w^+ represent the initial and final vibrational quantum numbers, respectively corresponding to the ground electronic state $X^1\Sigma^+$ of ArH^+ .

The manuscript is organized as follows: in Section 2, the theoretical model used to characterize the ArH^{**} resonant states is presented and in Section 3 the results concerning the cross-sections and the corresponding rate coefficients are discussed. Finally, the conclusions, in Section 4, close the paper.

2 THEORETICAL MODEL

A theoretical study of the ArH^+ electronic excited states was performed by Stolyarov & Child (2005); Jungen, Roche & Arif (1997), and more recently Kirrander, Child & Stolyarov (2006), explored ArH Rydberg states.

In this work, *ab initio* ArH^+ calculations were performed using MOLPRO and an aug-cc-pVQZ (AVQZ) Gaussian-type orbital (GTO) basis set at the complete active space (CAS) self-consistent field (SCF) level of theory. These calculations provided input orbitals for the electron-ion scattering calculations. All calculations were performed in C_{2v} symmetry, which is the highest allowed by MOLPRO and the polyatomic R-matrix code for an asymmetric linear molecule.

The potential energy curves and the widths for the ArH^{**} resonant states were calculated using the R-matrix method (Tennyson 2010) as implemented in UKRMol code (Carr et al. 2012). The general approach follows closely the treatment of N_2^{**} by Little & Tennyson (2014) which provided the input for N_2^+ DR calculations (Little et al. 2014). The ArH^+ target states were represented using the AVQZ GTO basis set and a CAS in which the $\text{Ar } 1s^2 2s^2 2p^6$ electrons were frozen and the remaining eight electrons were distributed as $(4\sigma, 5\sigma, 6\sigma, 2\pi)^8$. The 3π virtual orbital was retained to augment the continuum orbitals in the scattering calculation.

The scattering calculations used an R-matrix sphere of radius $10 a_0$. Continuum basis functions were represented using GTOs placed at the centre of this sphere and contained up to g orbitals ($\ell \leq 4$) (Faure et al. 2002). Close-coupling calculations built on the target CAS (Tennyson 1996) and an expansion of the eight lowest states of each (C_{2v}) symmetry were retained for the outer region calculations. In this latter region, calculations were repeated for the internuclear separations $2.2 < R < 15 a_0$ and for symmetries corresponding to $^2\Sigma^+$, $^2\Pi$ and $^2\Delta$ scattering channels.

The outer region calculations explicitly considered the 20 lowest target states. R-matrices were propagated to $100.1 a_0$ and then fitted to an asymptotic form. Resonance positions and widths were determined by automated fitting of the eigenphase sums to a Breit-Wigner form using program RESON (Tennyson & Noble 1984). Couplings were determined from the resonance widths Γ using the formula:

$$V(R) = \sqrt{\frac{\Gamma(R)}{2\pi}}. \quad (3)$$

Fig. 1 shows the R-matrix results for resonance positions (upper panel), couplings (middle panel) and quantum defect (lower panel). The corresponding molecular data are given in Table 1. These data form the input for the Multichannel Quantum Defect Theory (MQDT) step of the calculations. Linear extrapolation was

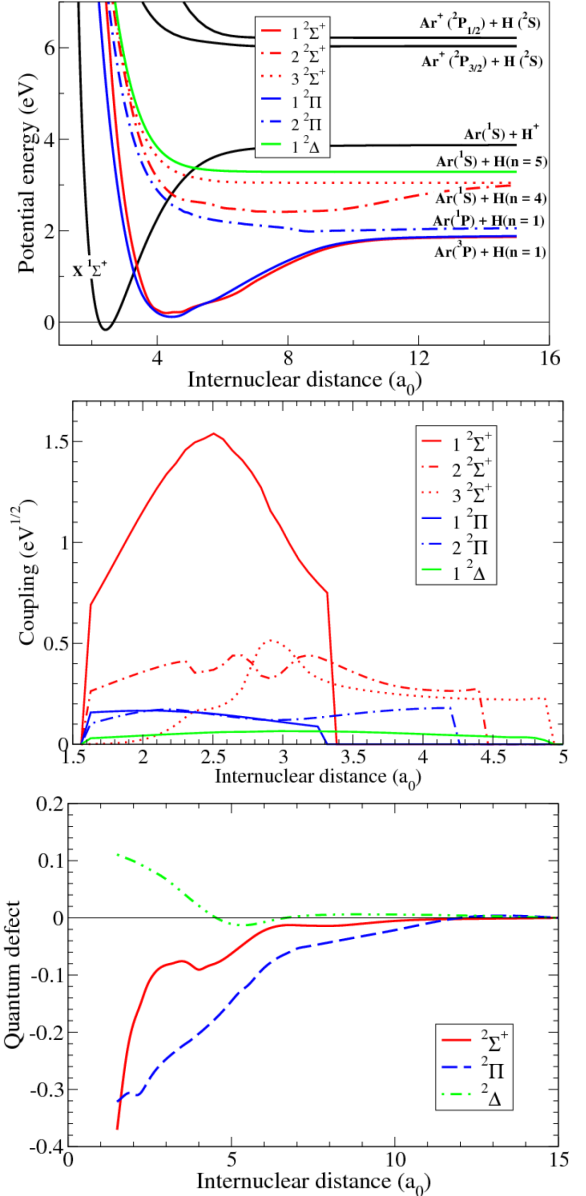


Figure 1. Potential energy curves, couplings, and quantum defects used in the present calculations. The ArH^+ potential curves – ground state, $X^1\Sigma^+$, and the lowest excited electronic states – are displayed as black lines. The molecular data sets for the different symmetries of the neutral system are displayed with different colours: $^2\Sigma$ in red, $^2\Pi$ in blue, and $^2\Delta$ in green.

adopted for the couplings in order to extend the internuclear distances range below $2.2 a_0$ to $1.6 a_0$.

ArH^+ is a closed-shell system, so no spin-orbit (SO) splitting effects are expected in its ro-vibrational levels. Conversely, SO effects may be important in the non- Σ resonances and are well characterized for the Ar asymptotic states. In particular, the $\text{Ar}(^2P_{3/2}^0 4s)$ and $\text{Ar}(^2P_{1/2}^0 4s)$ show SO splittings of 0.075 eV and 0.105 eV, respectively (Kramida et al. 2018). Our calculations are non-relativistic and therefore neglect SO effects; we assume the calculated R-matrix resonances converge on the lowest component of the Ar doublets at large internuclear distances. Table 2 shows the asymptotic limits of the ArH^{**} resonant states considered below.

The MQDT method (Giusti 1980; Guberman & Giusti-Suzor 1991; Chakrabarti et al. 2013; Little et al. 2014; Motapon et al.

Table 1. Molecular constants (reduced mass, equilibrium distance, and dissociating energies) for ⁴⁰ArH⁺ in its ground electronic state and the energies of the corresponding vibrational levels. The comparison with the experimental data of Hotop et al. (1998) given in brackets is reported.

μ (a.u.)	1791.94		
R_{eq} (a_0)	2.419 (2.419)		
D_e (eV)	4.039 (4.025)		
D_0 (eV)	3.8725		
v^+	ϵ_{v^+} (eV)	v^+	ϵ_{v^+} (eV)
0	0.000	12	2.949
1	0.321	13	3.110
2	0.627	14	3.258
3	0.919	15	3.393
4	1.197	16	3.513
5	1.461	17	3.617
6	1.712	18	3.703
7	1.949	19	3.770
8	2.174	20	3.817
9	2.387	21	3.846
10	2.587	22	3.861
11	2.774		

Table 2. Asymptotic limits of the ArH^{**} resonant states relevant for the low-energy impact collisions. The energy is expressed with respect to the asymptotic limit of the ground electronic state of ArH⁺. The experimental energy values from the NIST database (Kramida et al. 2018) are given in brackets for comparison.

Channel	Energy (eV)	Symmetries
Ar(³ P) + H($n = 1$)	-2.00 (-2.05)	$1^2\Sigma^+, 1^2\Pi$
Ar(¹ P) + H($n = 1$)	-1.81 (-1.87)	$2^2\Pi$
Ar(¹ S) + H($n = 4$)	-0.87 (-0.85)	$2^2\Sigma^+, 3^2\Sigma^+$
Ar(¹ S) + H($n = 5$)	-0.58 (-0.54)	$1^2\Delta$

2014; Epée Epée et al. 2015) was used to study the processes (1) and (2). Within this approach, the corresponding cross-sections are expressed in terms of S-matrix elements as:

$$\sigma_{v^+}(\epsilon) = \frac{\pi}{4\epsilon} \sum_{\text{sym}, \Lambda, l, j} \rho^{\text{sym}, \Lambda} \left| S_{d_j, l v^+}^{\text{sym}, \Lambda} \right|^2, \quad (4)$$

$$\sigma_{v^+, w^+}(\epsilon) = \frac{\pi}{4\epsilon} \sum_{\text{sym}, \Lambda, l, l'} \rho^{\text{sym}, \Lambda} \left| S_{l' w^+, l v^+}^{\text{sym}, \Lambda} - \delta_{l, l'} \delta_{v^+, w^+} \right|^2, \quad (5)$$

where the summation is extended over all symmetries (sym: spin, inversion for homonuclear molecules) of the neutral system, projection of the total electronic angular momentum on the internuclear axis Λ , and partial waves l/l' of the incident/scattered electron, and $\rho^{\text{sym}, \Lambda}$ is the ratio between the multiplicities of the neutral system and of the target ion.

The most abundant isotope of argon in the Earth's atmosphere is ⁴⁰Ar whereas in the ISM ³⁶Ar and ³⁸Ar isotopes are preponderant. In this work, we deal with vibrational processes and, due to the small relative variation of the reduced mass from one isotopologue to another – as a consequence of the huge atomic mass of the Ar isotopes – we expect these effects to be negligible. In order to verify this, we performed calculations for different isotopologues of ArH⁺ and the relative difference between the rate coefficients was found to be below 1 per cent.

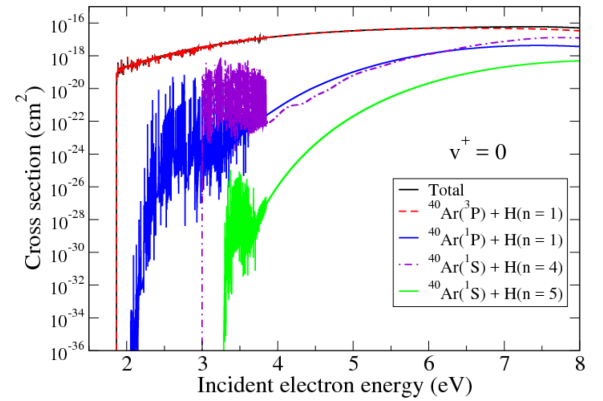


Figure 2. Dissociative recombination of vibrationally relaxed ArH⁺. Broken coloured lines: The contributions coming from all the dissociative states having the same asymptotic atomic limit. Solid black line (partially hidden by the red curve): Total cross-section coming from the sum over all the available dissociative states.

3 RESULTS AND DISCUSSION

Fig. 2 displays the DR cross-sections for ArH⁺ $v^+ = 0$, namely the total one and the partial contributions corresponding to the asymptotic channels of resonant states. It can be noted that the main contribution arises from the Ar(³P) + H($n = 1$) channel. One reason for this is that, as shown in Table 2, this exit channel gathers contributions coming from two states - $1^2\Sigma^+$ and $1^2\Pi$ – instead of one state, as is the case of the exit channels Ar(¹P) + H($n = 1$) and Ar(¹S) + H($n = 5$). One can argue that – as shown in Table 2 – the channel Ar(¹S) + H($n = 4$) is the asymptotic limit of two states, as the Ar(³P) + H($n = 1$) one. However, the coupling of the $1^2\Sigma^+$ state with the electron/ion continuum (see Fig. 1) is about three times larger than the other ones.

Figs 3(a) and (b) display, respectively, the results for DR cross-sections and the corresponding rate coefficients for $v^+ = 0, 1, 2$. Two features can be noted:

(i) The resonant structures present in the cross-sections correspond to the temporary captures into singly-excited Rydberg states ArH^{*}, and they cease to appear when the electron energy reaches the dissociation energy of ArH⁺ ($v^+ = 0, 1, 2$);

(ii) For a vibrationally relaxed target, the dissociation channels are closed for energies of the incident electron below 1.8 eV. For the ion situated on one of the next isg8 excited vibrational states, the threshold decreases progressively, and the DR becomes exothermic for vibrational levels equal or higher to 9 only. This particular energetic situation explains the particular behavior of the computed rate coefficients displayed in Fig. 3(b), namely the very low values and the ‘explosive’ increase below 2000 K.

In order to validate the results, Fig. 4 shows the anisotropic DR rate coefficient for $v^+ = 0$, calculated by considering the electron beam with a longitudinal temperature $kT_{\parallel} \approx 0.5$ eV and a transverse temperature $kT_{\perp} \approx 25$ meV, compared to the experimental data from the storage ring by Mitchell et al. (2005). We note that the agreement is quite satisfactory at energies greater than ~ 3 eV within the 20 per cent experimental error. At lower energies, our calculated rates are smaller than the experimental ones: This can derive from bad detected signal as stated by the authors.

Fig. 5 displays the DR cross-section compared to the competitive process of VE for one quantum excitation in the same energy range. The main feature is that, at energies just above the opening of

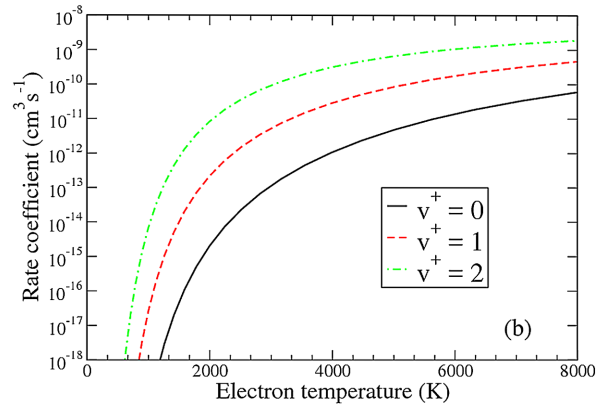
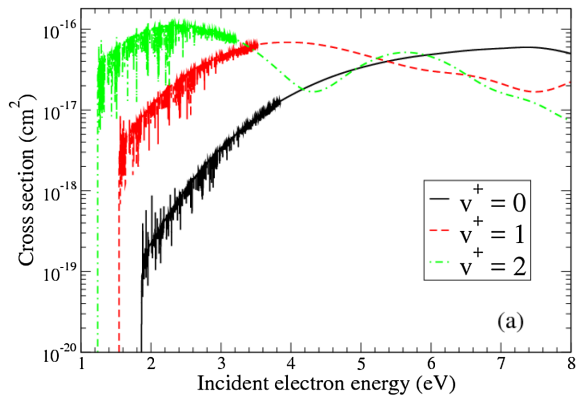


Figure 3. Dissociative recombination of ArH^+ on its lowest vibrational levels: (a) global cross-sections, coming from the sum over all the available dissociative states; (b) the corresponding Maxwellian-averaged rate coefficients.

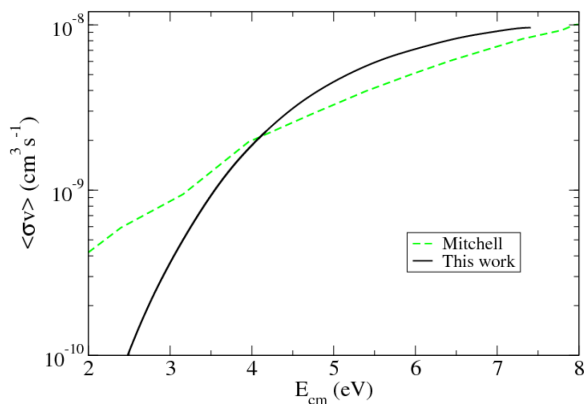


Figure 4. Dissociative recombination of vibrationally relaxed ArH^+ . Comparison between the rate coefficient measured in the CRYRING storage ring Mitchell et al. (2005) and the anisotropic rate coefficient obtained by the convolution of our MQDT-computed cross-section using the temperatures characterizing the relative velocities of the electrons with respect to the ions in the experiment.

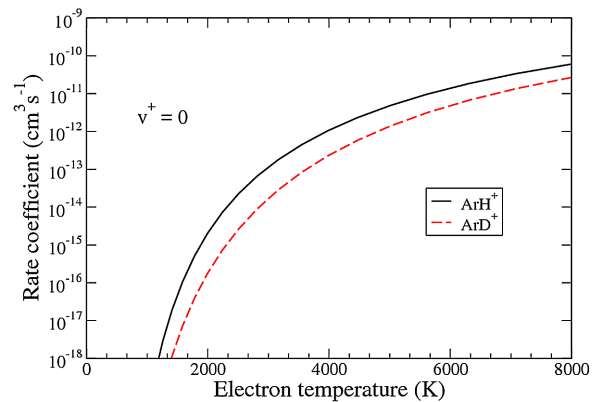


Figure 6. Dissociative recombination rate of vibrationally relaxed ArH^+ and ArD^+ as a function of electron temperature: The isotopic effects.

Fig. 6 displays this effect for $v^+ = 0$ DR rate coefficient. The rates decrease by a factor between 10 at 1000K and 3 at 8000K, due to lowering of the ArD^+ ground state, compared to that of ArH^+ .

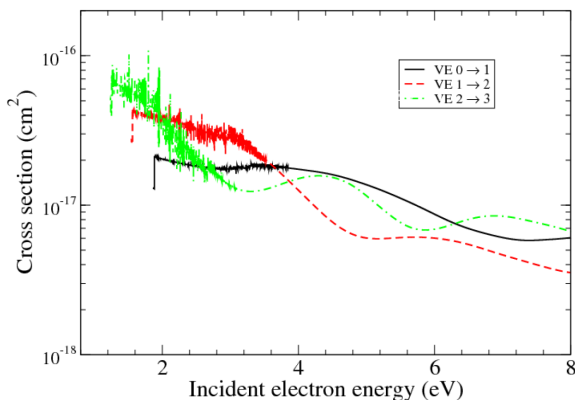


Figure 5. Vibrational excitation (VE) of ArH^+ on its lowest vibrational levels: Cross-sections for $\Delta v^+ = 0$ (solid lines). The dissociative recombination (DR) cross-section are also shown for comparison (broken line).

the dissociative channels, the VE cross-section is larger than the corresponding DR starting from the same vibrational level.

We also checked the isotopic effect by replacing ArH^+ by ArD^+ , which results in a variation of the reduced mass by a factor of 2.

3.1 Astrophysical consequences

As stated previously, ArH^+ DR is an important destruction mechanism in interstellar conditions. We have examined two different environments where this molecular ion has been found and have varied the value of the DR rate coefficient over a range of values between 10^{-9} and 10^{-18} $\text{cm}^3 \text{s}^{-1}$ for a sample of 0D steady-state chemical models. We solve the coupled $\frac{d}{dt}[X] = 0$ differential equations where $[X]$ stands for the abundance of a particular X molecule included in the chemical network for a fixed value of density and temperature and different values of the DR chemical rate coefficient of ArH^+ , $k_{\text{DR}}(\text{ArH}^+)$. In Fig. 7(a), we display the different solutions of the argonium relative abundance as a function of $k_{\text{DR}}(\text{ArH}^+)$ for typical diffuse cloud conditions: Proton density $n_{\text{H}} = 100 \text{ cm}^{-3}$, temperature $T = 100 \text{ K}$, H_2 cosmic ionization rate $\zeta = 10^{-16} \text{ s}^{-1}$, visual extinction $A_v = 0.001$, and standard interstellar radiation field defined by the scaling parameter $\chi = 1$. In Fig. 7(b), we display the different solutions for physical conditions pertaining to the Crab nebula, as discussed in Priestley et al. (2017), i.e. $n_{\text{H}} = 2000 \text{ cm}^{-3}$, $T = 1000 \text{ K}$, H_2 cosmic ionization rate $\zeta = 5 \cdot 10^{-10} \text{ s}^{-1}$, $\chi = 60$, $A_v = 0.1$ and the elemental abundances displayed in Table 1 of Priestley et al. (2017). Each point corresponds to a specific

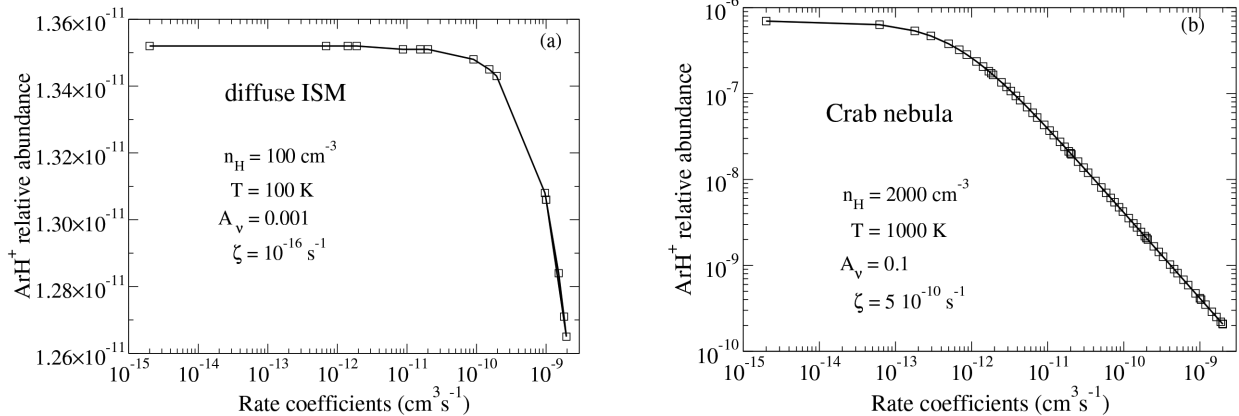


Figure 7. Relative abundance of ArH⁺ as a function of the rate coefficients for the case of (a) diffuse ISM (temperature $T = 100 \text{ K}$) and (b) Crab nebula (temperature $T = 1000 \text{ K}$).

model result and the line connects the different model results. In the standard diffuse cloud conditions, we see that the argonium relative abundance remains constant for values of k_{DR} (ArH⁺) smaller than some $10^{-11} \text{ cm}^3 \text{ s}^{-1}$, where another destruction mechanism such as photodissociation becomes dominant. It should also be noticed that the scale is linear and the variations are moderate. However, in the extreme conditions of the Crab nebula where the cosmic ionization rate is about 7 orders of magnitude larger, the variation of the relative fractional abundance of argonium is much more spectacular. The limiting value of k_{DR} (ArH⁺) = $10^{-13} \text{ cm}^3 \text{ s}^{-1}$, below which the relative abundance of argonium remains almost stable and the destruction by photodissociation and reaction with H₂ take over the dissociative recombination. Our theoretical computations demonstrate that the actual value is significantly below the experimental upper limit $10^{-9} \text{ cm}^3 \text{ s}^{-1}$ and even below the limiting values stressed out by the models (see Fig. 3(b)). Within these findings, we conclude that DR plays a negligible role in astrophysical media and that photodissociation and reactions with molecular hydrogen become the main destruction processes.

4 CONCLUSIONS

In this paper, we explored the superexcited states of ArH within the R-matrix approach and we computed the cross-sections and the corresponding rate coefficients for the dissociative recombination and the vibrational excitation of ArH⁺ by using Multichannel Quantum Defect Theory. The very low values of the dissociative recombination rate coefficients leads to the conclusion that the only significant ArH⁺ destruction mechanisms in the interstellar medium are the collisions with H₂ molecules and the photodissociation.

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APPENDIX A: SOME EXTRA MATERIAL

The numerical data for ArH^+ dissociative recombination rate coefficients corresponding to the Fig. 3(b) can be found as supplementary material to this paper.

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